

C. Vyšetřete (absolutní/neabsolutní) konvergenci řad.

1.

$$\sum_{k=1}^{\infty} \frac{\sin kx}{2^k}$$

10.

$$\sum_{k=1}^{\infty} (-1)^k \frac{\sin^2 k}{k}$$

2.

$$\sum_{k=1}^{\infty} (-1)^{\frac{k(k+1)}{2}} \frac{1}{\sqrt[3]{k}}$$

11.

$$\sum_{k=2}^{\infty} \frac{1}{\ln^2 k} \cos \frac{\pi k^2}{k+1}$$

3.

$$\sum_{k=1}^{\infty} 2^k \sin \frac{x}{3^k}$$

12.

$$\sum_{k=1}^{\infty} (-1)^k \frac{k-1}{k+1} \frac{1}{\sqrt[100]{k}}$$

4.

$$\sum_{k=1}^{\infty} (-1)^k \frac{2 + (-1)^k}{k}$$

13.

$$\sum_{k=1}^{\infty} \frac{(-1)^k}{k^p}$$

5.

$$\sum_{k=1}^{\infty} (-1)^k \left(1 + \frac{1}{k}\right)^{k^2} \frac{1}{e^k}$$

14.

$$\sum_{k=1}^{\infty} \frac{\sin kx}{k^p}, \quad 0 < x < \pi$$

6.

$$\sum_{k=1}^{\infty} \sin(\pi \sqrt{x^2 + k^2})$$

15.

$$\sum_{k=1}^{\infty} (-1)^{k-1} \frac{1}{k^{p+\frac{1}{n}}}$$

7.

$$\sum_{k=10}^{\infty} (-1)^k \frac{\sqrt[k]{k}}{\ln \ln \ln k}$$

16.

$$\sum_{k=1}^{\infty} \frac{\sin \frac{k\pi}{4}}{\sin \frac{k\pi}{4} + k^p}$$

8.

$$\sum_{k=1}^{\infty} \frac{(\ln k)^{100}}{k} \sin \frac{k\pi}{4}$$

17.

$$\sum_{k=1}^{\infty} (-1)^{k-1} \left(\frac{1 \cdot 3 \cdots (2n-1)}{2 \cdot 4 \cdots 2n} \right)^p$$

9.

$$\sum_{k=2}^{\infty} \frac{\sin(k + \frac{1}{k})}{\ln \ln k}$$