NMAG 405 - Universal Algebra 1 - fall semester 2019/20Homework 5

Deadline 07.01.2019, 11:30

1. (10 points) Let $C = Clo(\mathbf{A})$, where $\mathbf{A} = (\{1, 2, 3, 4\}, *)$ with

*		2		4
1	2	$ \begin{array}{c} 3 \\ 4 \\ 1 \\ 4 \end{array} $	2	1
2	1	4	3	4
3	2	1	2	1
4	3	4	3	2

- (a) Prove that there is no 5-ary operation $f \in \mathcal{C}$ satisfying f(4, 2, 4, 4, 4) = 1
- (b) Prove that there is no 5-ary operation $f\in \mathcal{C}$ satisfying f(2,1,3,4,3)=1 and f(2,1,1,4,3)=2

(Hint: invariant relations)

- 2. (10 points) Let $\mathbf{L} = (\{0, 1, 2\}, \wedge, \vee)$ be the three-element lattice. Find a monotone idempotent operation that is not in $Clo(\mathbf{L})$.
- 3. (10 points) In the lecture you saw that C = Pol(Inv(C)), if C is a clone on some finite set A. Show that for clones on an infinite A this is not true in general (Hint: study the clone generated by all bijections $A \to A$).