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"Symplectic decomposition, Darboux theorem and ellipticity"

Our first result concerns the classical Darboux theorem. We prove that if  $\omega_m$  is the standard symplectic form and  $f$  is a symplectic form, then we can find a diffeomorphism  $\varphi$ , with optimal regularity, satisfying

$$\varphi^*(\omega_m) = f \quad \text{and} \quad \delta[\varphi \lrcorner \omega_m] = 0$$

provided that  $f$  is a small perturbation of  $\omega_m$ . Moreover we show that the above system is elliptic and that we have uniqueness, when coupled with a Dirichlet datum.

We then apply the above result to the so-called symplectic decomposition. We show that any map  $\varphi$ , satisfying appropriate assumptions, can be written as

$$\varphi = \psi \circ \chi$$

where

$$\psi^*(\omega_m) = \omega_m \quad \text{and} \quad \delta[\chi \lrcorner \omega_m] = d\chi \lrcorner \omega_m = 0.$$

The analogy with mass transportation and the Monge-Ampère equation, as well as with the polar decomposition, will be emphasized.

This is a joint work with Wifrid GANGBO and Olivier KNEUSS.