

TOPIC 03

Solve the following problems in the real domain.

- (1) $2 \cos x + 1 = 0$ $[\pm \frac{2}{3}\pi + 2k\pi]$
- (2) $(3 \cos x + 7)(-2 \sin x - 1) = 0$ $[-\frac{1}{6}\pi + 2k\pi, \frac{5}{6}\pi + 2k\pi]$
- (3) $(6 \tan 2x - 2)(2 \tan 2x - 6) = 0$ $[\frac{1}{2} \arctan \frac{1}{3} + \frac{1}{2}k\pi, \frac{1}{2} \arctan 3 + \frac{1}{2}k\pi]$
- (4) $\sin 2x = -\sin(-x)$ $[k\pi, \pm \frac{1}{3}\pi + 2k\pi]$
- (5) $\sin x + \sqrt{3} \cos x = 2$ $[\frac{1}{6}\pi + 2k\pi]$
- (6) $4 \sin^3 x + 4 \sin^2 x - 3 \sin x = 3$
- (7) $[\frac{1}{3}\pi + 2k\pi, \frac{2}{3}\pi + 2k\pi, \frac{4}{3}\pi + 2k\pi, \frac{3}{2}\pi + 2k\pi, \frac{5}{3}\pi + 2k\pi]$
- (8) $\tan(-x + \frac{\pi}{6}) = \sqrt{3}$ $[-\frac{\pi}{6} + k\pi]$
- (9) $2|\cos x| = \sin^2 x$ $[\pm \arccos(\sqrt{2} - 1) + k\pi]$
- (10) $\cos |x| = \sin x$ $[\frac{1}{4}\pi + 2k\pi, \frac{5}{4}\pi + 2k\pi]$
- (11) $|\sin x| = \cos^2 x$ $[\pm \arcsin(\frac{1}{2}(\sqrt{5} - 1)) + k\pi]$
- (11) $\sin |x| = \cos x$ $[\frac{1}{4}\pi + 2k\pi, k \geq 0; \frac{5}{4}\pi + 2k\pi, k \geq 0; -\frac{1}{4}\pi + 2k\pi, k \leq 0; -\frac{5}{4}\pi + 2k\pi, k \leq 0]$

In all cases we assume $k \in \mathbf{Z}$.