

B. Vyšetřete spojitost funkce $F(a)$:

$$1. \int_0^{\infty} \frac{\exp(-ax)}{1+x^3} dx, \quad a \geq 0 \quad 2. \int_0^{\infty} \frac{x}{1+x^a} dx, \quad a > 2$$

$$3. \int_0^{\pi} \frac{\sin x}{x^a(\pi-x)^a} dx, \quad a < 2 \quad 4. \int_{-1}^1 \sqrt{x^2+a^2}, \quad a \in R$$

$$5. \int_0^{\infty} \exp(-ax) \frac{\sin x}{x} dx, \quad a > 0 \quad 6. \int_1^{\infty} \frac{\sin\left(\frac{1}{x}\right)}{x(a+x)^2}, \quad a > -1$$

C. Derivováním podle parametru spočtěte integrály:

$$1. \int_0^{\infty} \frac{1 - \exp(-ax^2)}{x^2 \exp(x^2)} dx \quad 2. \int_0^1 \frac{x^a - 1}{\ln x} dx$$

$$3. \int_0^{\infty} \exp(-x) \frac{\sin(ax)}{x} dx \quad 4. \int_0^{\infty} \exp(-x) \frac{1 - \cos(ax)}{x} dx$$

$$5. \int_0^{\infty} \frac{\operatorname{arctg}(ax)}{x(1+x^2)} dx \quad * 6. \int_0^{\infty} \exp\left\{-x^2 - \frac{a^2}{x^2}\right\} dx$$

$$7. \int_0^{\pi/2} \frac{\ln(1+a \sin x)}{\sin x} dx \quad 8. \int_0^{\pi} \frac{\ln(1+\cos x)}{\cos x} dx$$