

A. Pomocí podílového, odmocninového nebo Raabeho kritéria vyšetřete:

1.

$$\sum_{k=1}^{\infty} \frac{2^k}{k!}$$

6.

$$\sum_{k=1}^{\infty} \frac{k!}{k^{k+p}}$$

2.

$$\sum_{k=1}^{\infty} \frac{(k!)^2}{(2k)!}$$

7.

$$\sum_{k=1}^{\infty} \frac{k^k}{(2k^2 + k + 1)^{\frac{k}{2}}}$$

3.

$$\sum_{k=1}^{\infty} \frac{k^{ak}}{k!}$$

8.

$$\sum_{k=1}^{\infty} \frac{2 \cdot 5 \cdot 8 \cdots (3k-1)}{1 \cdot 5 \cdot 9 \cdots (4k-3)}$$

4.

$$\sum_{k=1}^{\infty} \frac{(k!)^2}{2^{k^2}}$$

9.

$$\sum_{k=1}^{\infty} \frac{p(p+1) \cdots (p+k-1)}{k!} \frac{1}{k^q}$$

5.

$$\sum_{k=1}^{\infty} \frac{k^2}{\left(\frac{\pi}{3} + \frac{1}{k}\right)^k}$$

10.

$$\sum_{k=1}^{\infty} \left( \frac{1 \cdot 3 \cdots (2k-1)}{2 \cdot 4 \cdots 2k} \right)^p$$

B. Pomocí srovnávacího a integrálního kritéria vyšetřete:

1.

$$\sum_{k=1}^{\infty} \frac{1}{\ln k}$$

7.

$$\sum_{k=1}^{\infty} (k^{(k^2+1)^{-1}} - 1)$$

2.

$$\sum_{k=1}^{\infty} \frac{k^2}{k^3 + 1}$$

8.

$$\sum_{k=1}^{\infty} e^{-\sqrt[3]{k}}$$

3.

$$\sum_{k=1}^{\infty} \frac{2k^2 + 3k + 4}{(2k^2 + 5)^2}$$

9.

$$\sum_{k=1}^{\infty} \frac{1}{k^a \ln^b k}$$

4.

$$\sum_{k=1}^{\infty} \frac{1}{\sqrt{2k+1}\sqrt{2k+3}}$$

10.

$$\sum_{k=1}^{\infty} n^3(1 - \cos n^{-1})$$

5.

$$\sum_{k=1}^{\infty} \frac{\sqrt{k+2} - \sqrt{k-2}}{k^a}$$

11.

$$\sum_{k=1}^{\infty} \sin n^{-1} \ln \frac{n+1}{n}$$

6.

$$\sum_{k=1}^{\infty} (k^{k^a} - 1)$$

12.

$$\sum_{k=1}^{\infty} \sin \frac{n}{n^2 + 1}$$