

$$\lim_{n \rightarrow \infty} (n^2 + \sin(n+1)) \cdot (\sqrt{n^4+2} - \sqrt{n^4+1}) \cdot \frac{(\sqrt{n^4+2} + \sqrt{n^4+1})}{(\sqrt{n^4+2} + \sqrt{n^4+1})} =$$

$$= \lim_{n \rightarrow \infty} \frac{(n^2 + \sin(n+1)) \cdot (n^4 + 2 - n^4 - 1)}{(\sqrt{n^4+2} + \sqrt{n^4+1})} = \lim_{n \rightarrow \infty} \frac{n^2 \cdot (1 + \frac{\sin(n+1)}{n^2})}{(\sqrt{1 + \frac{2}{n^4}} + \sqrt{1 + \frac{1}{n^4}})} \stackrel{\text{VOAL}}{=}$$

$$\neq \frac{\lim_{n \rightarrow \infty} (1 + \frac{\sin(n+1)}{n^2})}{\lim_{n \rightarrow \infty} (\sqrt{1 + \frac{2}{n^4}} + \sqrt{1 + \frac{1}{n^4}})} \stackrel{\text{VOAL}}{=} \frac{\lim_{n \rightarrow \infty} 1 + \lim_{n \rightarrow \infty} (\sin(n+1) \cdot \frac{1}{n^2})}{\lim_{n \rightarrow \infty} \sqrt{1 + \frac{2}{n^4}} + \lim_{n \rightarrow \infty} \sqrt{1 + \frac{1}{n^4}}} =$$

$$\left( \begin{array}{l} \bullet \lim_{n \rightarrow \infty} \frac{1}{n^2} = 0 \text{ protože } \lim_{n \rightarrow \infty} \frac{1}{n^2} = \lim_{n \rightarrow \infty} \frac{1}{n} \cdot \frac{1}{n} \stackrel{\text{VOAL}}{=} \lim_{n \rightarrow \infty} \frac{1}{n} \cdot \lim_{n \rightarrow \infty} \frac{1}{n} = 0 \cdot 0 = 0 \\ \bullet \lim_{n \rightarrow \infty} \frac{1}{n^4} = 0 \text{ protože } \lim_{n \rightarrow \infty} \frac{1}{n^4} = \lim_{n \rightarrow \infty} \frac{1}{n^2} \cdot \frac{1}{n^2} \stackrel{\text{VOAL}}{=} \lim_{n \rightarrow \infty} \frac{1}{n^2} \cdot \lim_{n \rightarrow \infty} \frac{1}{n^2} = 0 \cdot 0 = 0 \end{array} \right)$$

• Věta o mizející a omezené posloupnosti:  $\lim_{n \rightarrow \infty} a_n \cdot b_n = 0$   
pro  $a_n$  mizející a  $b_n$  omezenou posl.

$$\lim_{n \rightarrow \infty} \sin(n+1) \cdot \frac{1}{n^2} = 0$$

$\downarrow$   $\downarrow$   
 $a_n$   $b_n$  mizející

~~lim\_{n \rightarrow \infty} \sin(n+1) = 0~~  
~~lim\_{n \rightarrow \infty} \frac{1}{n^2} = 0~~

$$= \frac{1 + 0}{\lim_{n \rightarrow \infty} \sqrt{1 + \frac{2}{n^4}} + \lim_{n \rightarrow \infty} \sqrt{1 + \frac{1}{n^4}}} \stackrel{\text{VOAL}}{=} \frac{1}{\sqrt{\lim_{n \rightarrow \infty} (1 + \frac{2}{n^4})} + \sqrt{\lim_{n \rightarrow \infty} (1 + \frac{1}{n^4})}} = \frac{1}{\sqrt{1} + \sqrt{1}} = \frac{1}{2}$$

Věta o limitě odmocniny

$$1 + \frac{2}{n^4} > 0$$

$$1 + \frac{1}{n^4} > 0$$