

**Problem (Evans).** Let  $d \in \mathbb{R}$ ,  $T > 0$ ,  $f \in L^2((0, T) \times (0, 1))$ ,  $g \in W_0^{1,2}((0, 1))$ ,  $h \in L^2(0, 1)$ .  
Formulate a definition of a weak solution to the problem

$$u_{tt} + du_t - u_{xx} = f \quad \text{in } (0, T) \times (0, 1), \quad (1)$$

$$u = 0 \quad \text{on } ([0, T] \times \{0\}) \cup ([0, T] \times \{1\}), \quad (2)$$

$$u = g, u_t = h \quad \text{on } \{t = 0\} \times (0, 1). \quad (3)$$

Show there exists at most one weak solution of this initial/boundary-value problem. If necessary add a condition on  $d$ .