

Exam test A

Mathematics 1, WS 2017/18

1. (15 points) Compute the limit

$$\lim_{x \rightarrow 1} \left(\frac{1 + x^2}{4 - 2x} \right)^{\frac{x}{\sin(\pi x)}}.$$

2. (20 points) Investigate the function

$$f(x) = x^2 + \log(2 + x)$$

(find local extrema, intervals of monotonicity, convexity, inflections, limits in endpoints of D_f , asymptotes and draw graph of f).

3. (15 points) Investigate the function

$$g(x) = 2x^2 \operatorname{tg} x \operatorname{sgn}(\sin x - \frac{\sqrt{2}}{2})$$

in a neighborhood of $\frac{\pi}{4}$ (compute the limits of $g(x)$ and $g'(x)$ as $x \rightarrow \frac{\pi}{4}+$, $x \rightarrow \frac{\pi}{4}-$, decide, whether g is continuous at $\frac{\pi}{4}$, and draw graph of g in a neighborhood of $\frac{\pi}{4}$) and compute $g'_+(\frac{\pi}{4})$, $g'_-(\frac{\pi}{4})$.