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**Integral functionals  
that are continuous  
with respect to the  
weak topology on  $W_0^{1,p}(\Omega)$**

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