

Salvatore Leonardi, Jana Stará

**Regularity results for the gradient  
of solutions of linear elliptic systems  
with  $VMO$ -coefficients and  $L^{1,\lambda}$  data**

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Department of Mathematical Analysis, Faculty of Mathematics and Physics,  
Charles University, Sokolovská 83, 186 75 Praha 8, Czech Republic

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