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The sector of analycity of the Ornstein-Uhlenbeck semigroup on L^p spaces with respect to invariant measure

Preprint No. MATH-KMA-2004/126

January 2004

Submitted to *London Math. Society*

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Design by Mirko Rokyta, picture of snowflake by Ondřej Kalenda
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